

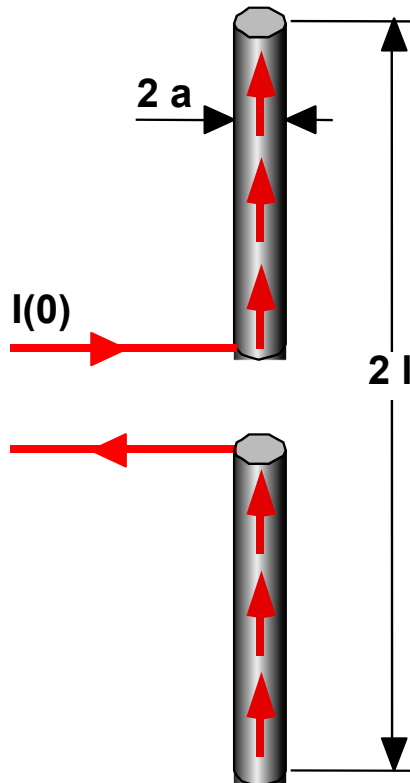
Stabstrahler

by Thomas Zwick

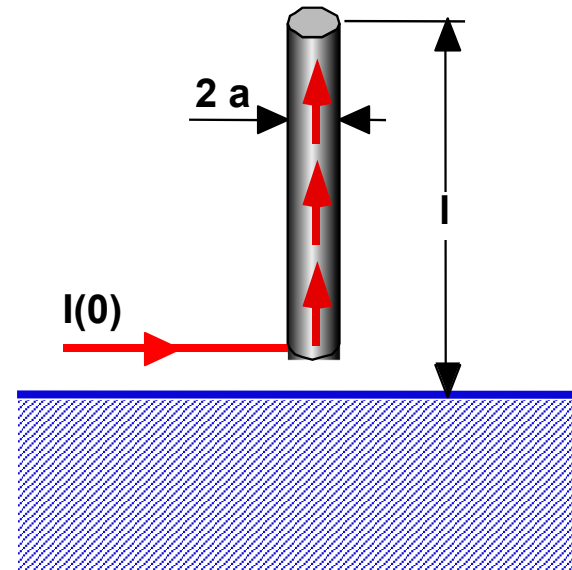
INSTITUT FÜR HOCHFREQUENZTECHNIK UND ELEKTRONIK



Dipol

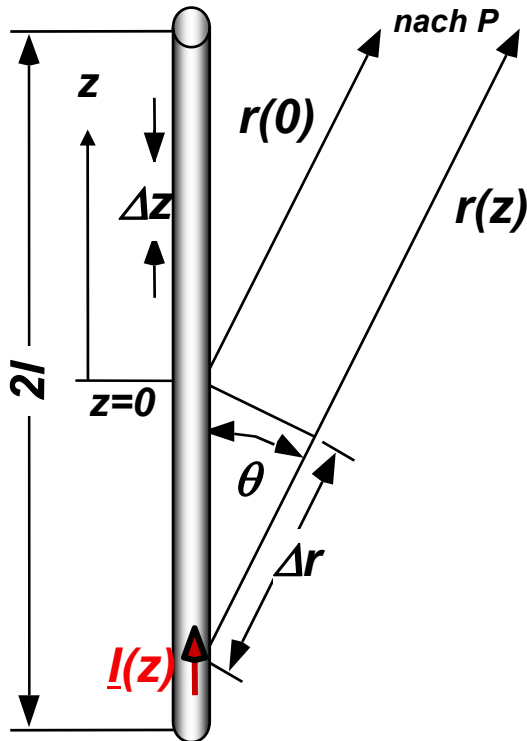


Monopol



Fernfeld von linearen Antennen

Geometrie



Elektrisches Fernfeld
des Hertz 'schen Dipols:

$$\underline{E}_{\theta HD} = I(z) dz \frac{\mu}{4\pi} \frac{e^{-j\beta r(z)}}{r(z)} j\omega \sin \theta$$

Elektrisches Fernfeld der linearen Antenne:

$$E_{\theta} = \iiint_V E_{\theta, HD}(\vec{r}) dV \quad E_{\theta} = \int_{-\ell}^{\ell} E_{\theta, HD}(z) dz$$

$$\underline{E}_{\theta} = \underbrace{j\omega \frac{\mu}{4\pi r} e^{-j\beta r(0)}}_{\text{Abstandsfaktor } A(r)} \underbrace{\sin \theta \int_{-\ell}^{\ell} \underline{I}(z) \cdot e^{j\beta z \cos \theta} dz}_{\text{und Richtungsfaktor } F(\theta) \text{ der Feldstärke}}$$

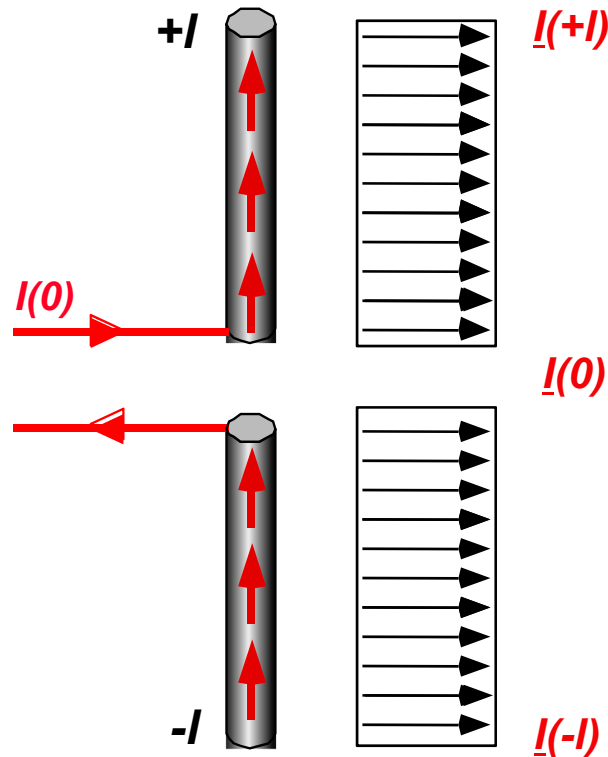
$$r(z) = r(0) + \Delta r$$

$$\Delta r = -z \cos(\theta)$$

Magnetisches Fernfeld der
linearen Antenne:

$$\underline{H}_{\psi} = \frac{\underline{E}_{\theta}}{Z_{F0}}$$

Stromverteilung



**Konstante
Stromverteilung:**

$$\underline{I}(z) = \underline{I}(0)$$

**Elektrisches Fernfeld der
linearen Antenne:**

$$\underline{E}_\theta = \underline{A}(r) \cdot \underline{F}(r)$$

Abstandsfaktor:

$$\underline{A}(r) = j\omega \frac{\mu}{4\pi r} e^{-j\beta r(0)}$$

Richtungsfaktor:

$$\underline{F}(r) = \sin \theta \int_{-\ell}^{\ell} \underline{I}(z) \cdot e^{j\beta z \cos \theta} dz$$

Linearer Stabstrahler mit homogener Stromverteilung

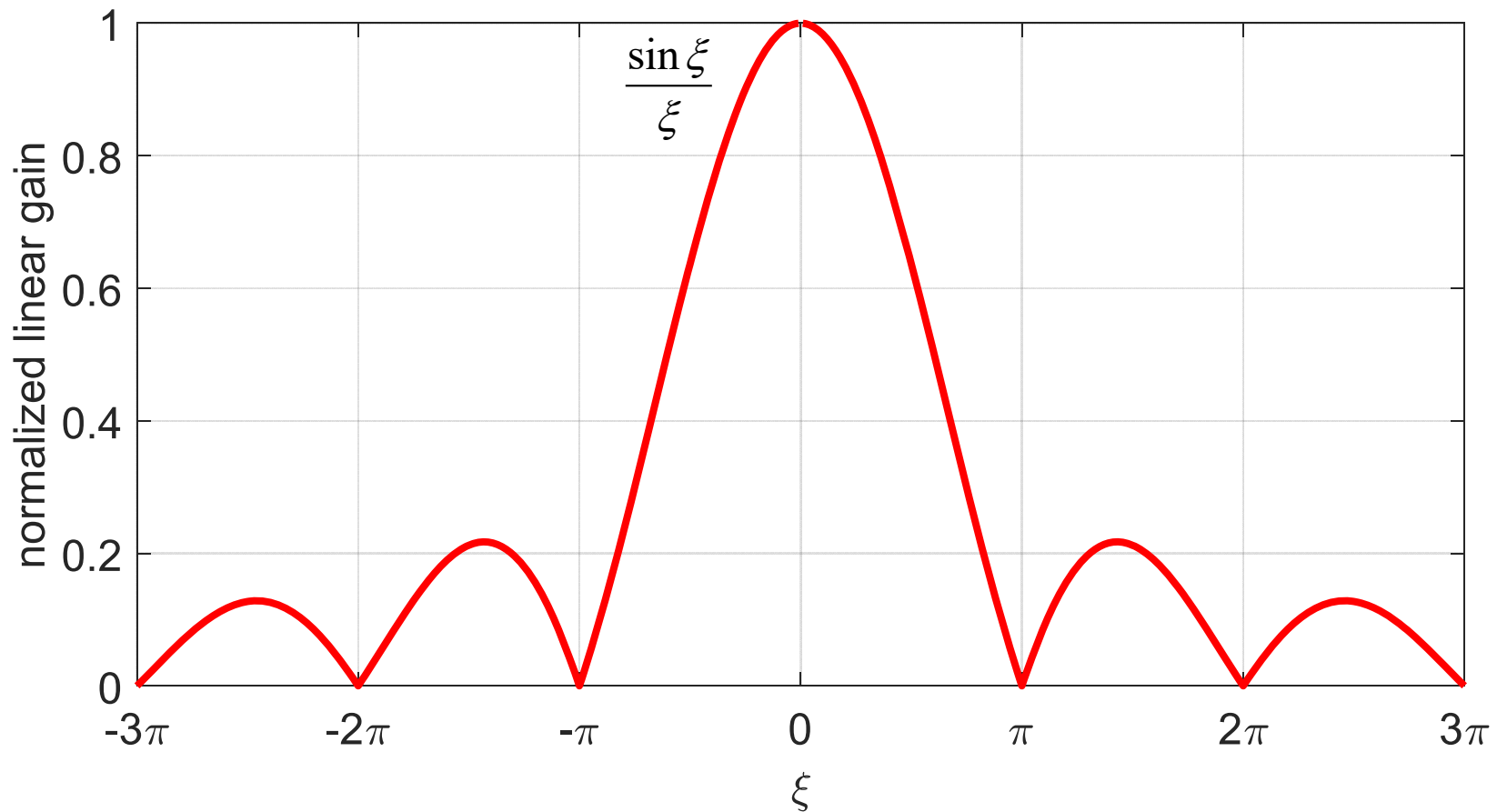
$$E_{\theta} = A(r) \sin \theta \int_{-\ell}^{\ell} I(0) \cdot e^{j\beta z \cos \theta} dz = A(r) I(0) \sin \theta \left[\frac{e^{j\beta z \cos \theta}}{j\beta \cos \theta} \right]_{-\ell}^{\ell} =$$
$$A(r) I(0) \sin \theta \frac{2j \sin(\beta \ell \cos \theta)}{j\beta \cos \theta} = A(r) I(0) 2\ell \sin \theta \frac{\sin \xi}{\xi} \quad \text{mit } \xi = \beta \ell \cos \theta$$

$$C(\theta) = \sin \theta \frac{\sin \xi}{\xi} \quad \text{Hauptstrahlrichtung: } \theta = \frac{\pi}{2}$$

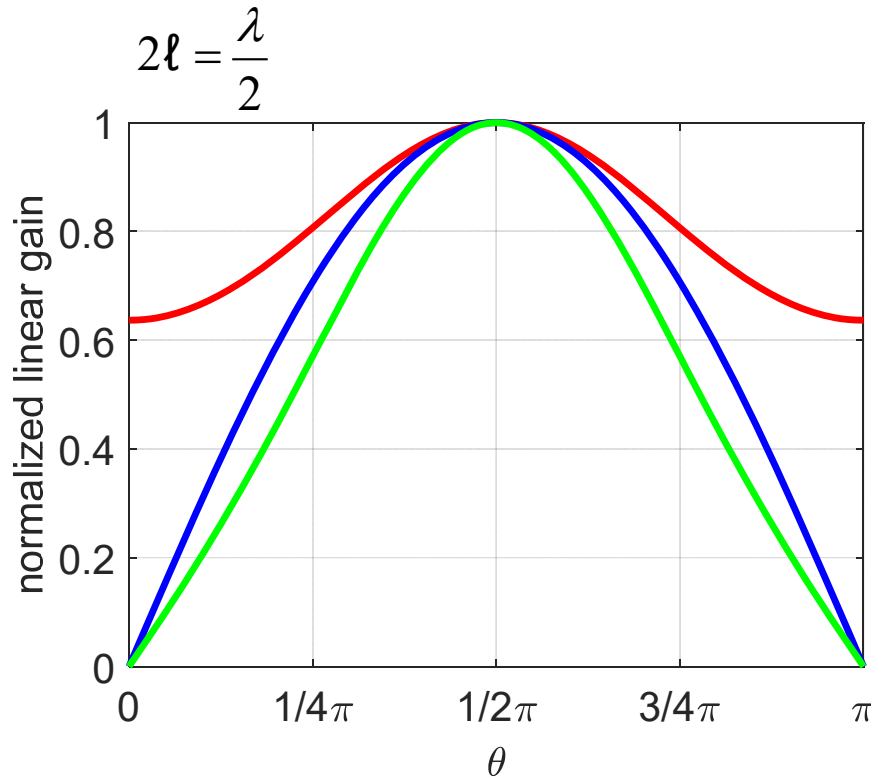
$$\text{Nullstellen: } \sin \theta = 0 \Rightarrow \theta = 0, \pi \quad \frac{\sin \xi}{\xi} = 0 \Rightarrow \frac{2\pi \ell}{\lambda} \cos \theta = n\pi$$

$$\text{Halbwertswinkel: } \frac{1}{\sqrt{2}} = \sin \theta \frac{\sin \xi}{\xi}$$

Richtdiagramm des Stabstrahlers mit homogener Belegung

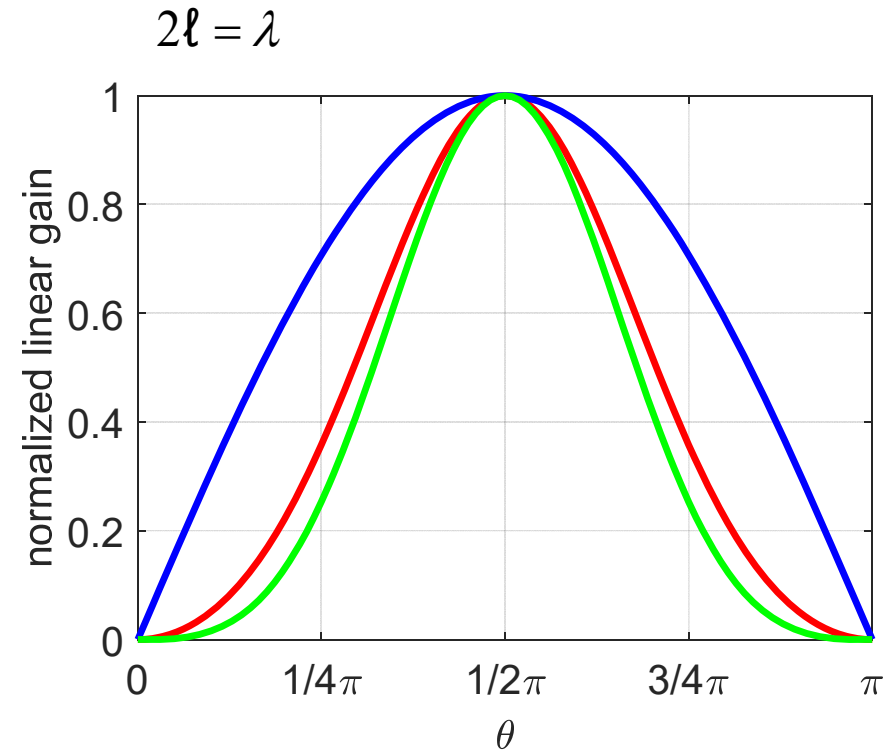


Richtdiagramm des Stabstrahlers mit homogener Belegung



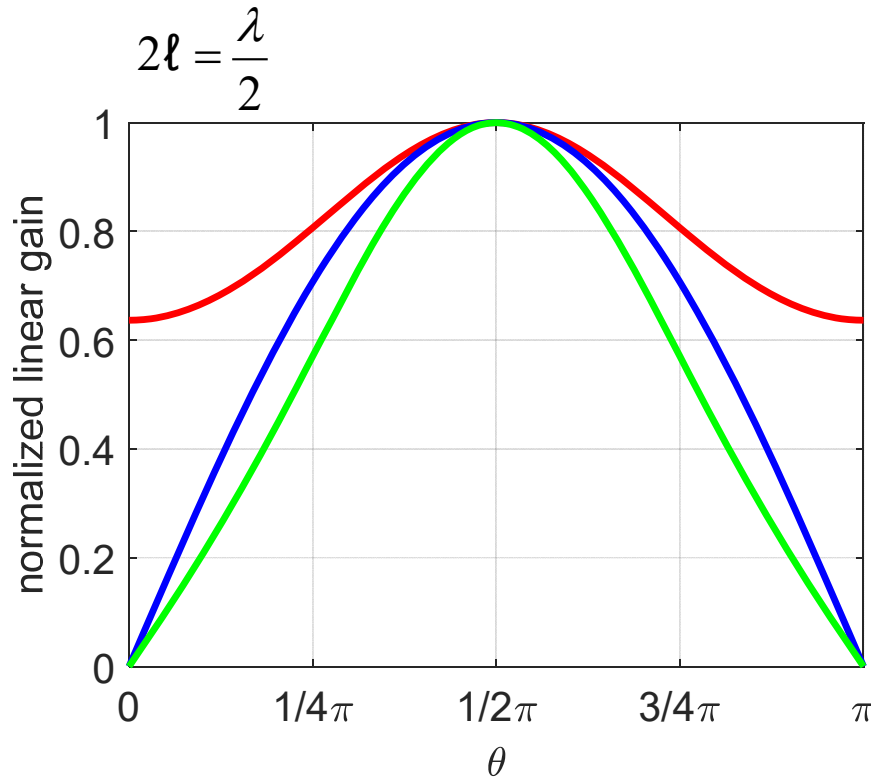
$$\frac{\sin \xi}{\xi} \text{ mit } \xi = \frac{2\pi\ell}{\lambda} \cos \theta$$

$$\sin \theta$$



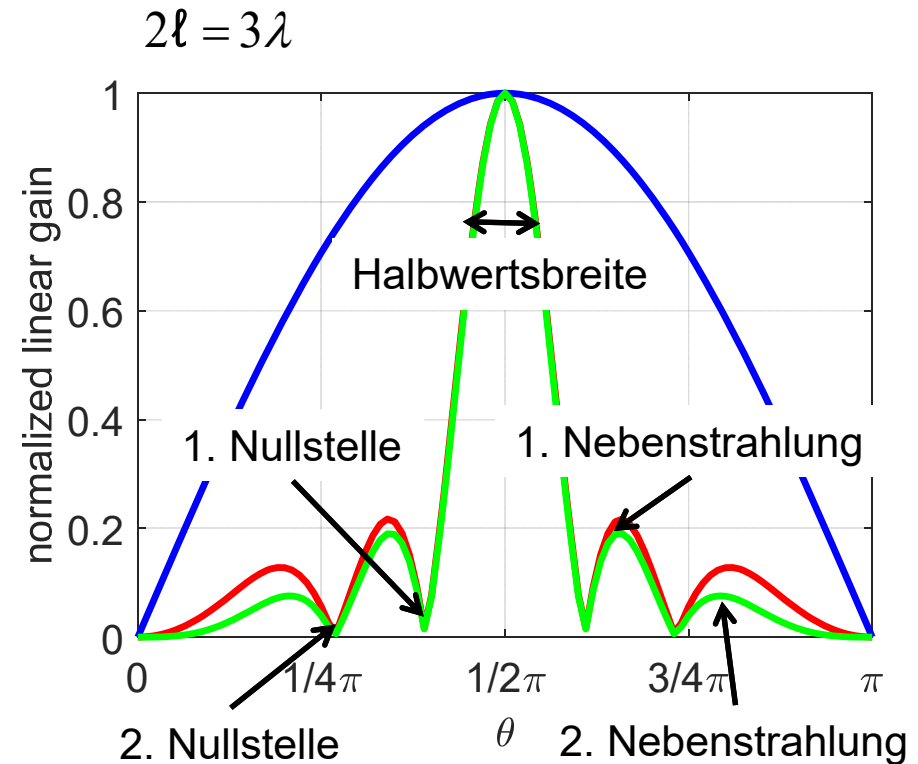
$$\sin \theta \frac{\sin \xi}{\xi} = \sin \theta \frac{\sin(\beta\ell \cos \theta)}{\beta\ell \cos \theta}$$

Richtdiagramm des Stabstrahlers mit homogener Belegung



$$\frac{\sin \xi}{\xi} \text{ mit } \xi = \frac{2\pi\ell}{\lambda} \cos \theta$$

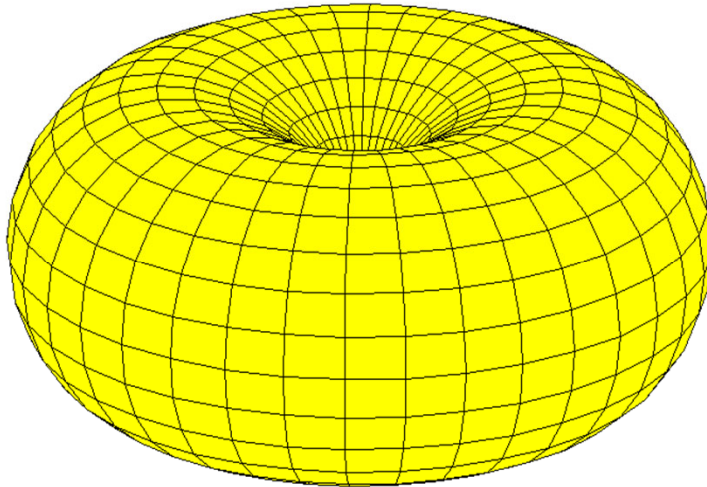
$$\sin \theta$$



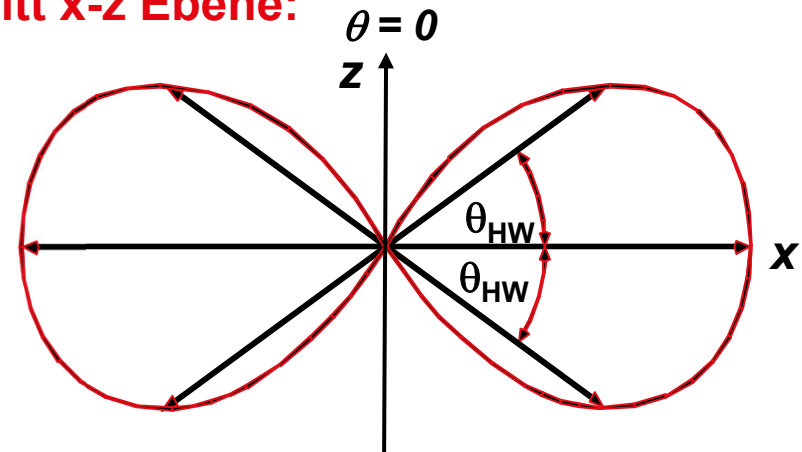
$$\sin \theta \frac{\sin \xi}{\xi} = \sin \theta \frac{\sin(\beta\ell \cos \theta)}{\beta\ell \cos \theta}$$

Vertikale Halbwertsbreite eines Stabstrahlers

3D:



Schnitt x-z Ebene:



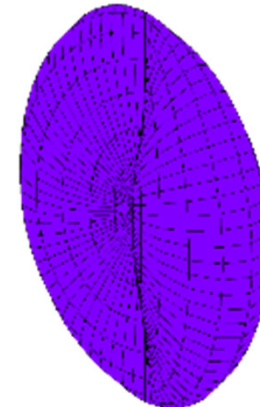
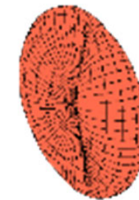
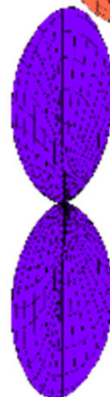
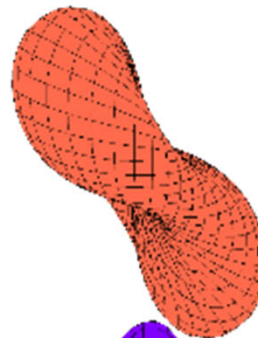
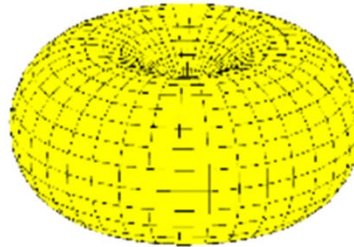
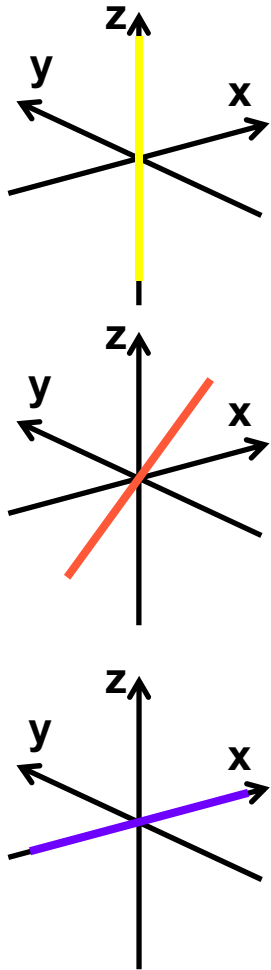
Halbwertswinkel θ_{HW} bei homogener Belegung:

$$\frac{1}{\sqrt{2}} = \sin \theta_{HW} \cdot \frac{\sin\left(\frac{2\pi\ell}{\lambda_0} \cos \theta_{HW}\right)}{\frac{2\pi\ell}{\lambda_0} \cos \theta_{HW}}$$

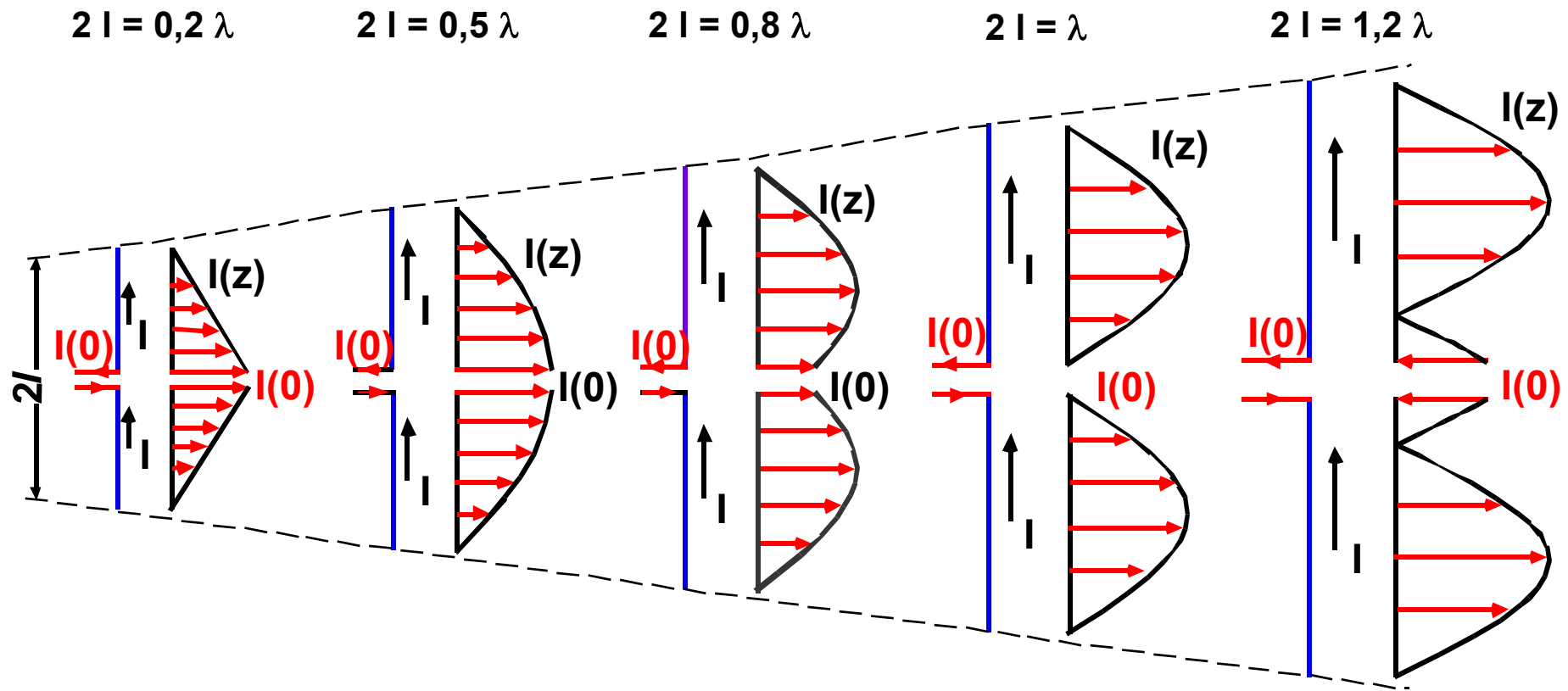
Einfluss des Koordinatensystems auf $C_\theta(\theta, \psi)$, $C_\psi(\theta, \psi)$

Richtcharakteristik $C_\theta(\theta, \psi)$

Richtcharakteristik $C_\psi(\theta, \psi)$



Reale Stromverteilung auf Stabstrahlern



Formeln Linearer Stabstrahler

$$E_{\theta} = j\omega \frac{\mu}{4\pi r} e^{-j\beta r(0)} \frac{I(0)}{\sin(\beta l)} \sin \theta \int_{-\ell}^{\ell} \sin(\beta(\ell - |z|)) \cdot e^{j\beta z \cos \theta} dz$$

$$\begin{aligned} \int_{-\ell}^{\ell} \sin(\beta(\ell - |z|)) \cdot e^{j\beta z \cos \theta} dz &= \int_{-\ell}^0 \sin(\beta(\ell + z)) \cdot e^{j\beta z \cos \theta} dz + \int_0^{\ell} \sin(\beta(\ell - z)) \cdot e^{j\beta z \cos \theta} dz = \\ &= \left[\frac{e^{j\beta z \cos \theta}}{-\beta^2 \cos^2 \theta + \beta^2} \{ j\beta \cos \theta \sin(\beta \ell + \beta z) - \beta \cos(\beta \ell + \beta z) \} \right]_{-\ell}^0 + \\ &+ \left[\frac{e^{j\beta z \cos \theta}}{-\beta^2 \cos^2 \theta + \beta^2} \{ j\beta \cos \theta \sin(\beta \ell - \beta z) + \beta \cos(\beta \ell - \beta z) \} \right]_0^{\ell} = \end{aligned}$$

Formelsammlung:

$$\int e^{\alpha x} \sin(\beta x + \gamma) dx = \frac{e^{\alpha x}}{\alpha^2 + \beta^2} [\alpha \sin(\beta x + \gamma) - \beta \cos(\beta x + \gamma)]$$

Formeln Linearer Stabstrahler

$$\begin{aligned}
 \int_{-\ell}^{\ell} \sin(\beta(\ell - |z|)) \cdot e^{j\beta z \cos \theta} dz &= \int_{-\ell}^0 \sin(\beta(\ell + z)) \cdot e^{j\beta z \cos \theta} dz + \int_0^{\ell} \sin(\beta(\ell - z)) \cdot e^{j\beta z \cos \theta} dz = \\
 &= \left[\frac{e^{j\beta z \cos \theta}}{-\beta^2 \cos^2 \theta + \beta^2} \{ j\beta \cos \theta \sin(\beta\ell + \beta z) - \beta \cos(\beta\ell + \beta z) \} \right]_{-\ell}^0 + \\
 &+ \left[\frac{e^{j\beta z \cos \theta}}{-\beta^2 \cos^2 \theta + \beta^2} \{ j\beta \cos \theta \sin(\beta\ell - \beta z) + \beta \cos(\beta\ell - \beta z) \} \right]_0^{\ell} = \\
 &= \frac{1}{\beta^2 \sin^2 \theta} \{ j\beta \cos \theta \sin(\beta\ell) - \beta \cos(\beta\ell) \} - \frac{e^{-j\beta\ell \cos \theta}}{\beta^2 \sin^2 \theta} \{ -\beta \} + \\
 &+ \frac{e^{j\beta\ell \cos \theta}}{\beta^2 \sin^2 \theta} \{ \beta \} - \frac{1}{\beta^2 \sin^2 \theta} \{ j\beta \cos \theta \sin(\beta\ell) + \beta \cos(\beta\ell) \} = \\
 &= \frac{e^{-j\beta\ell \cos \theta} + e^{j\beta\ell \cos \theta} - 2 \cos(\beta\ell)}{\beta \sin^2 \theta} = \frac{2 \cos(\beta\ell \cos \theta) - \cos(\beta\ell)}{\beta \sin^2 \theta}
 \end{aligned}$$

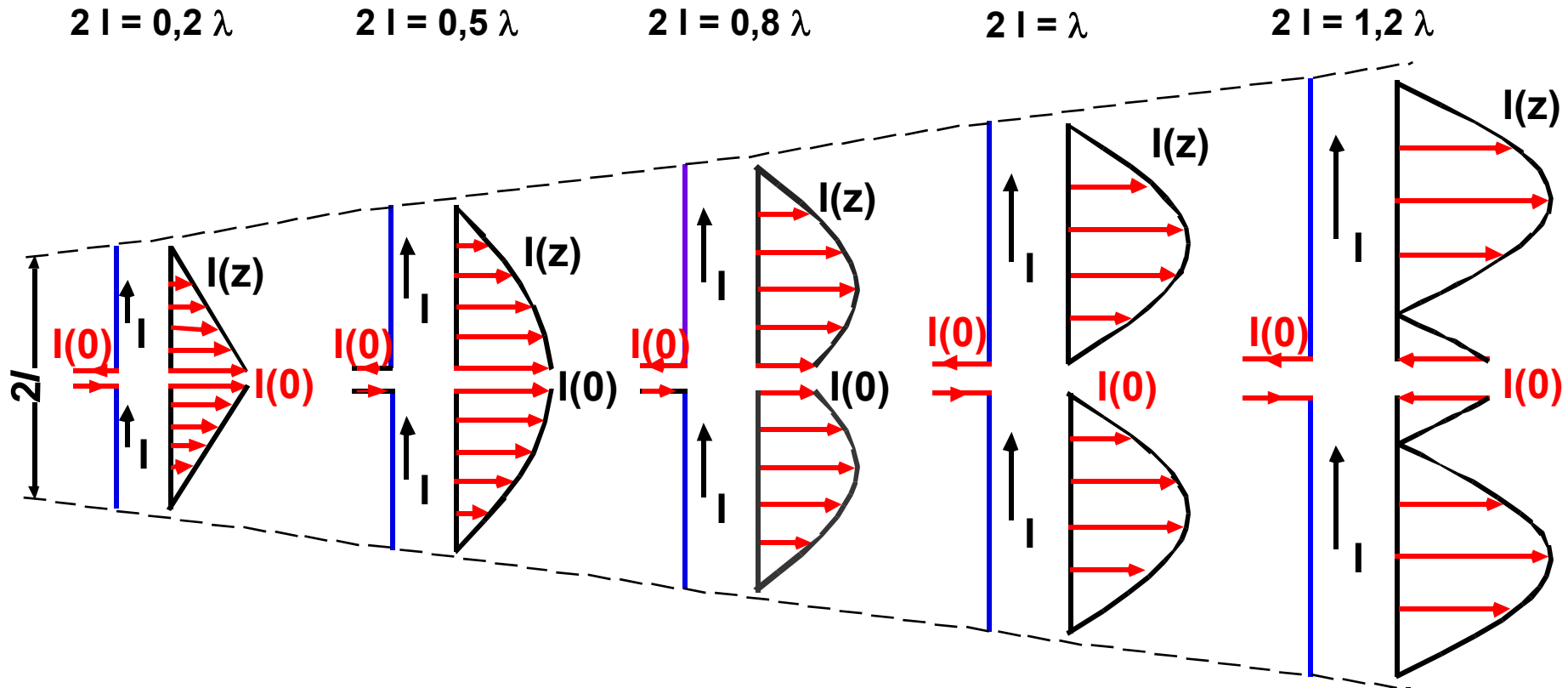
Formeln Linearer Stabstrahler

$$\int_{-\ell}^{\ell} \sin(\beta(\ell - |z|)) \cdot e^{j\beta z \cos \theta} dz = \frac{2}{\beta} \frac{\cos(\beta \ell \cos \theta) - \cos(\beta \ell)}{\sin^2 \theta}$$

$$I(z) = \frac{I(0)}{\sin(\beta \ell)} \sin(\beta(\ell - |z|)) \quad E_{\theta} = A(r) \frac{I(0)}{\sin(\beta \ell)} \sin \theta \int_{-\ell}^{\ell} \sin(\beta(\ell - |z|)) \cdot e^{j\beta z \cos \theta} dz$$

$$A(r) = j\omega \frac{\mu}{4\pi r} e^{-j\beta r(0)} \quad F(\theta) = \frac{I(0)}{\sin(\beta \ell)} \cdot \frac{2}{\beta} \cdot \frac{\cos(\beta \ell \cos \theta) - \cos(\beta \ell)}{\sin \theta}$$

Stromverteilung auf Stabstrahlern



$$I(z) = \frac{I(0)}{\sin(\beta\ell)} \sin(\beta(\ell - |z|)) \quad E_\theta = A(r) \frac{I(0)}{\sin(\beta\ell)} \sin\theta \int_{-\ell}^{\ell} \sin(\beta(\ell - |z|)) \cdot e^{j\beta z \cos\theta} dz$$

$$A(r) = j\omega \frac{\mu}{4\pi r} e^{-j\beta r(0)} \quad F(\theta) = \frac{I(0)}{\sin(\beta\ell)} \cdot \frac{2}{\beta} \cdot \frac{\cos(\beta\ell \cos\theta) - \cos(\beta\ell)}{\sin\theta}$$

$\lambda/2$ und λ -Dipol

$\lambda/2$ -Dipol:

$$2\ell = \frac{\lambda}{2} \Rightarrow \beta\ell = \frac{\pi}{2} \quad F(\theta) = \frac{2I(0)}{\beta} \cdot \frac{\cos\left(\frac{\pi}{2}\cos\theta\right)}{\sin\theta} \quad F_{\max} = \frac{2I(0)}{\beta} \text{ bei } \theta = \frac{\pi}{2} \Rightarrow C(\theta) = \frac{\cos\left(\frac{\pi}{2}\cos\theta\right)}{\sin\theta}$$

$$G_i = \frac{4\pi}{\int_{\psi=0}^{2\pi} \int_{\theta=0}^{\pi} C^2(\theta, \psi) \sin\theta \, d\theta \, d\psi} \approx 1.64 \, (2.15 \text{ dBi})$$

$$R_S = \frac{2P_T}{|I(0)|^2} \quad P_T = 4\pi r^2 \frac{|S|_{\max}}{G_i} \quad |S|_{\max} = \frac{|E_\theta|_{\max}^2}{2Z_{F0}} \quad |E_\theta|_{\max} = \frac{\omega\mu}{2\pi\beta r} |I(0)| = \frac{Z_{F0}}{2\pi r} |I(0)|$$

$$R_S = \frac{4\pi r^2 |E_\theta|_{\max}^2}{|I(0)|^2 G_i Z_{F0}} = \frac{Z_{F0}}{\pi G_i} = 73.2 \, \Omega$$

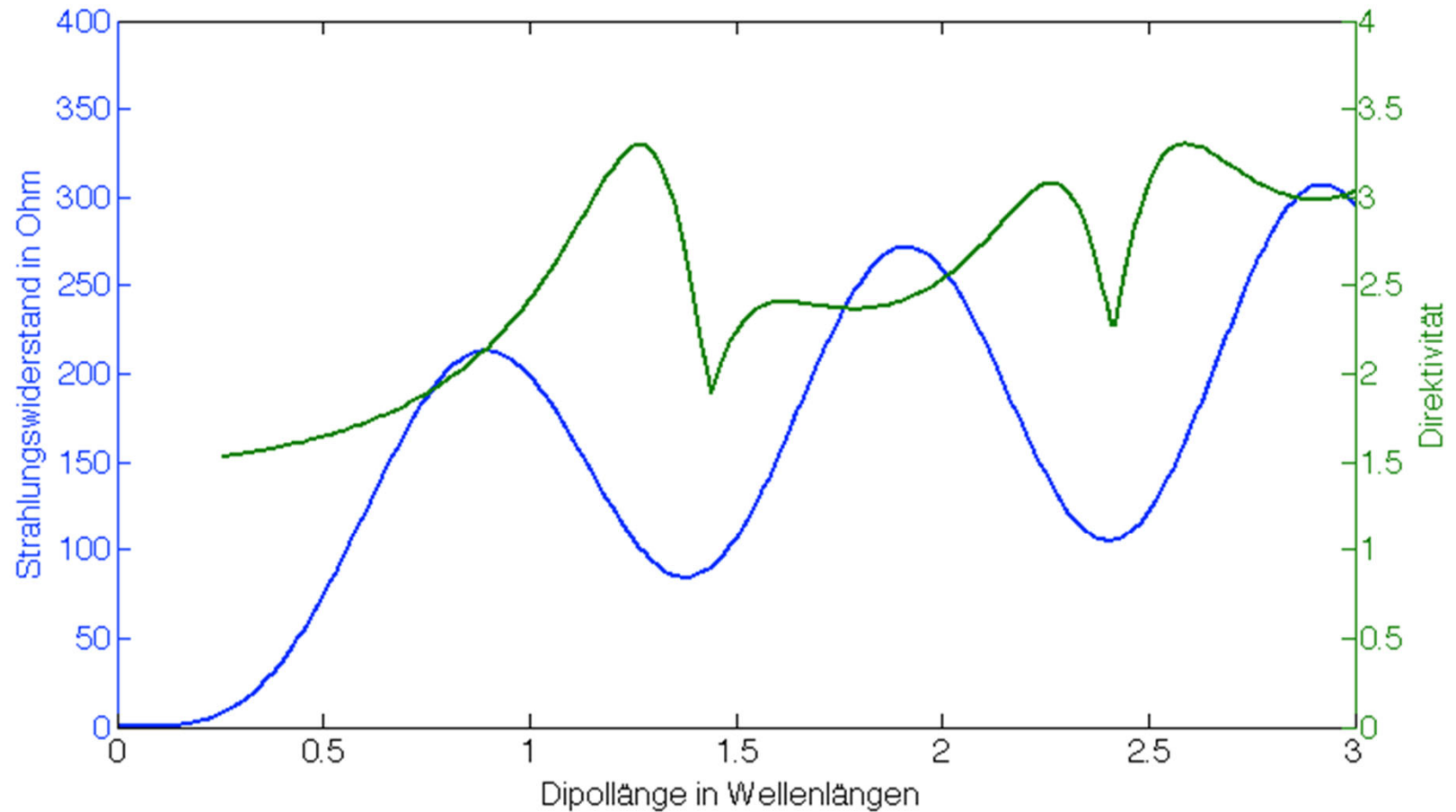
**Passt gut zu Coax-
Wellenwiderstand 75 Ω**

λ -Dipol:

$$2\ell = \lambda \Rightarrow \beta\ell = \pi \quad F_{\max} = \frac{I(0)}{\sin(\beta\ell)} \cdot \frac{2}{\beta} \cdot 2 \quad C(\theta) = \frac{F(\theta)}{F_{\max}} = \frac{\cos(\pi\cos\theta) + 1}{2\sin\theta}$$

numerische Auswertung: $G_i \approx 2.41 \, (3.82 \text{ dBi})$

Strahlungswiderstand und Direktivität



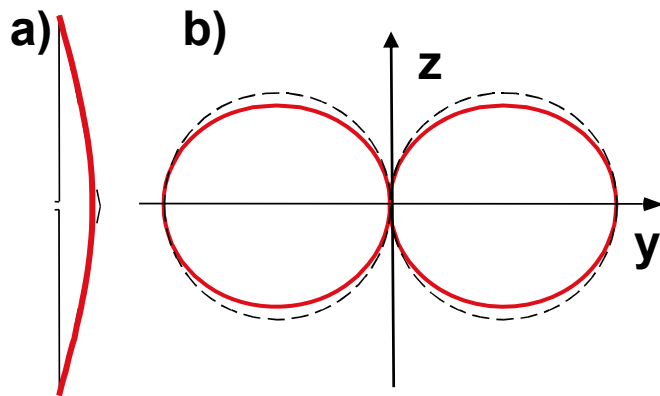
Dipol-Antennen

$\lambda/2$ - Dipol ($2l = \lambda/2$)

$$C(\theta, \psi) = \left| \frac{\cos\left(\frac{\pi}{2} \cos \theta\right)}{\sin \theta} \right|$$

G = 1.64 oder 2.15 dBi

$R_S = 73.2 \, \Omega$ $\theta_{HB} = 78^\circ$



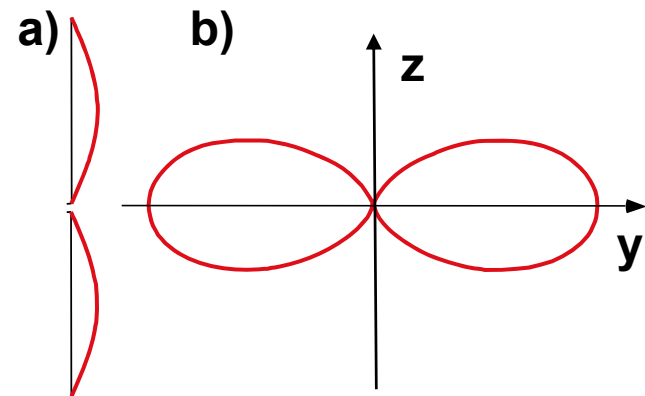
a) Stromverteilung
b) Richtch., Vergleich zum Hertzschen
Dipole (- - -)

λ - Dipol ($2l = \lambda$)

$$C(\theta, \psi) = \left| \frac{1}{2} \cdot \frac{\cos(\pi \cos \theta) + 1}{\sin \theta} \right|$$

G = 2.41 oder 3.82 dBi

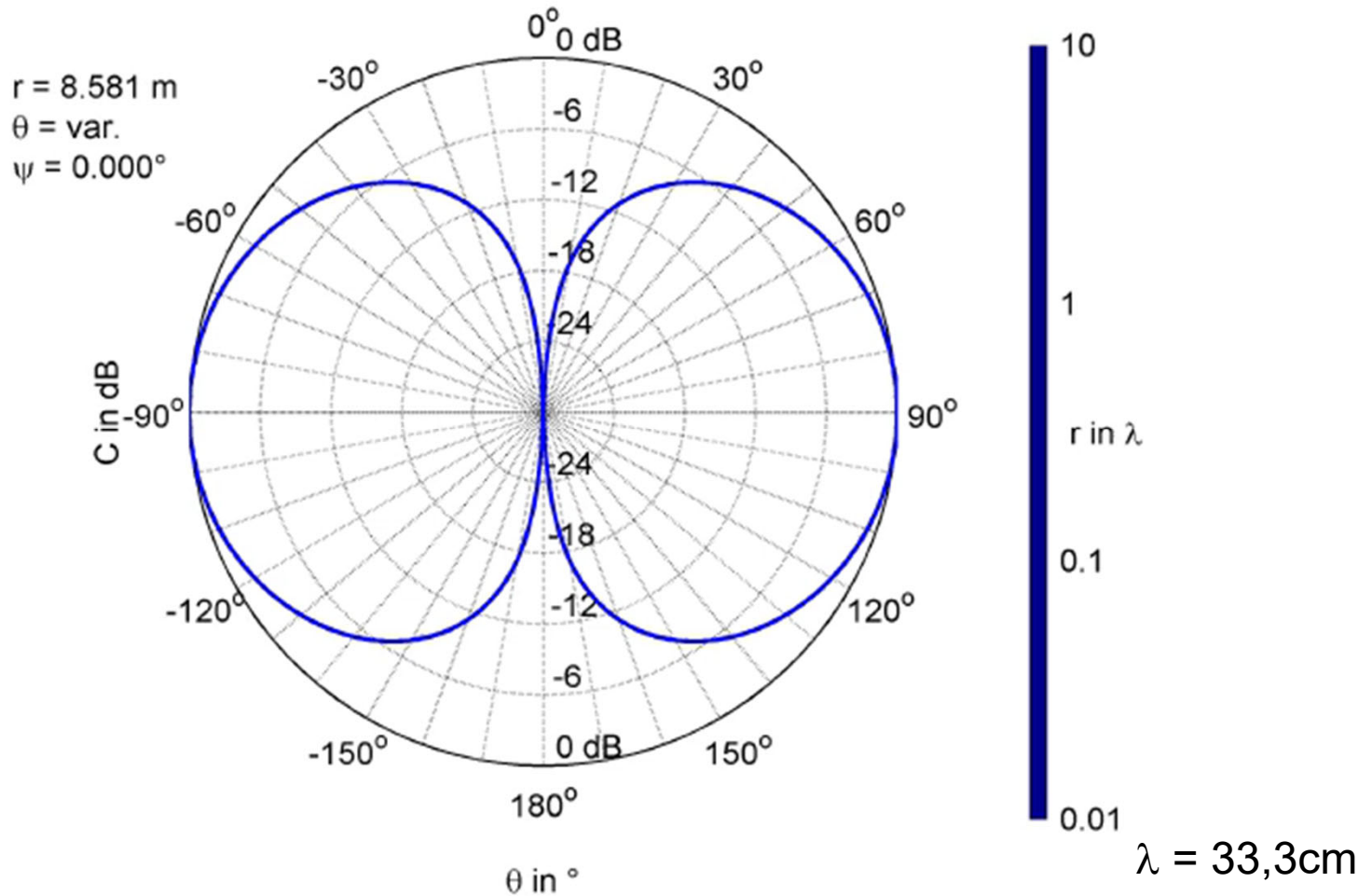
$R_S = 200 \, \Omega$ $\theta_{HB} = 47^\circ$



a) Stromverteilung
b) Richtcharakteristik

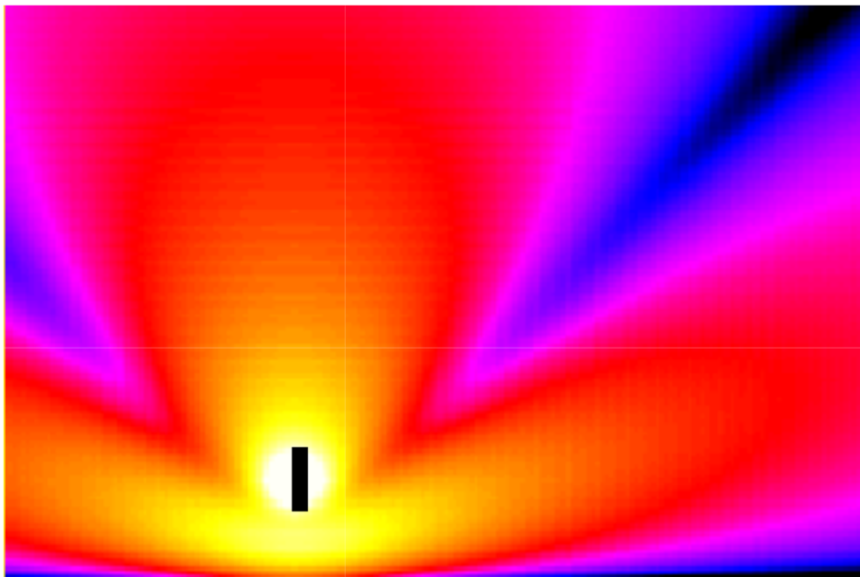
Elektr. Nahfeld Richtcharakteristik einer Dipolantenne

in z-Richtung orientierter $\lambda / 2$ -Dipol, $f = 900 \text{ MHz}$



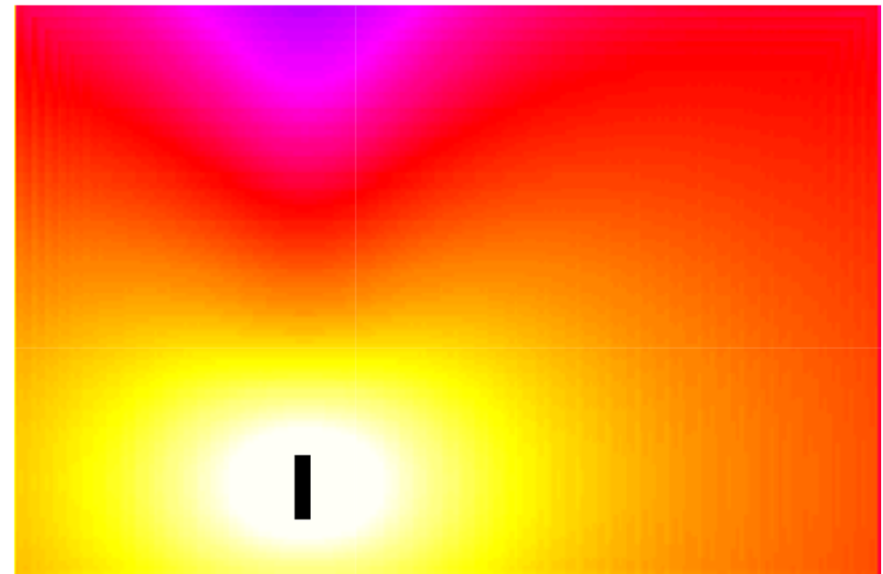
Feldstärken eines $\lambda/2$ -Dipols

Dipol im Freiraum über metallischem Boden



$|E|_{\text{norm}}$
0 dB -20 dB

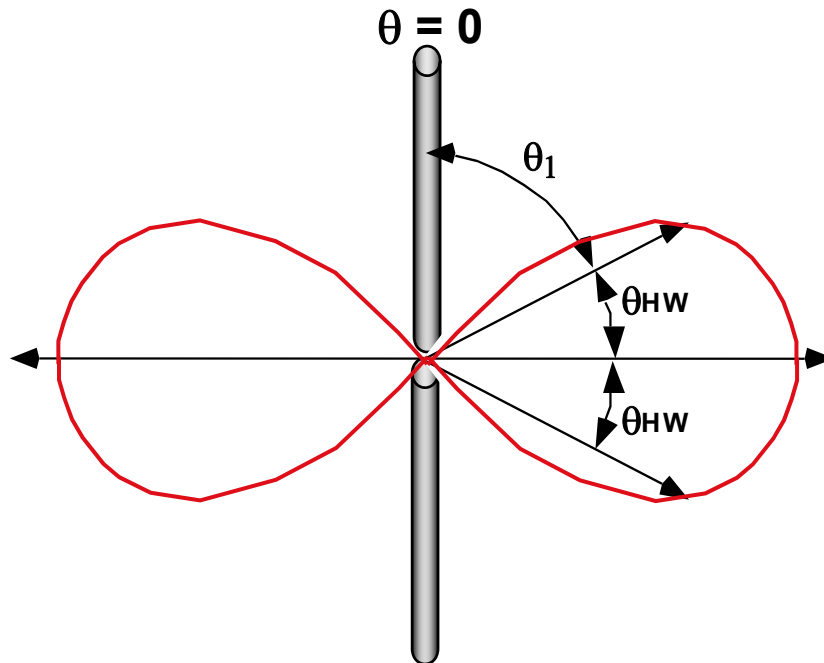
Dipol im Freiraum



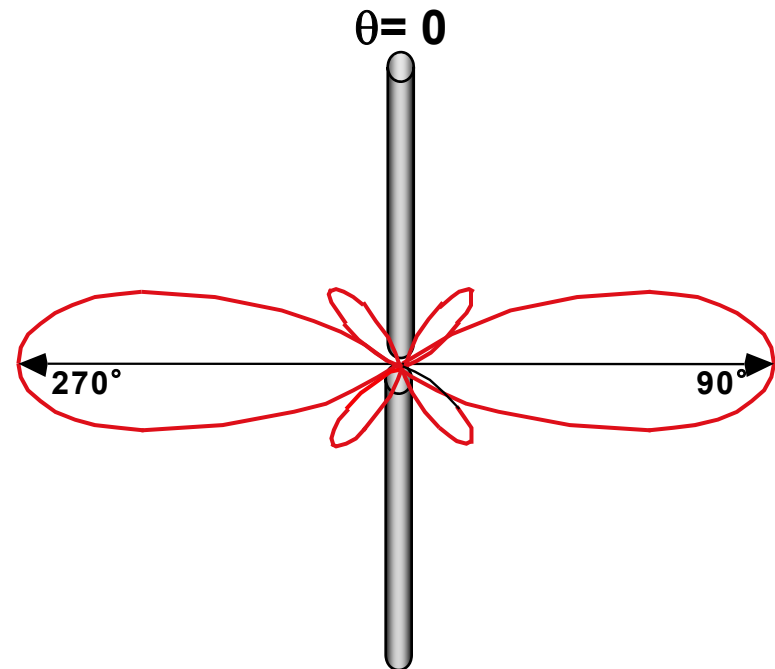
Frequenz 200 MHz, vertikale Polarisation, Dipolhöhe über Grund 2.5 m

Vertikale Halbwertsbreite eines Stabstrahlers

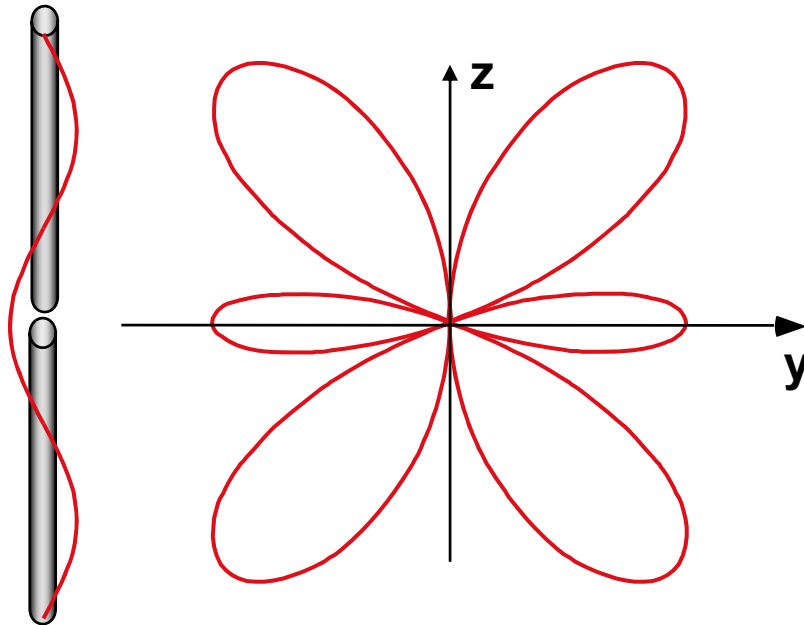
Stabstrahler mit $2l < \lambda_0$



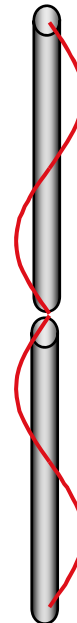
Stabstrahler mit $2l > \lambda_0$



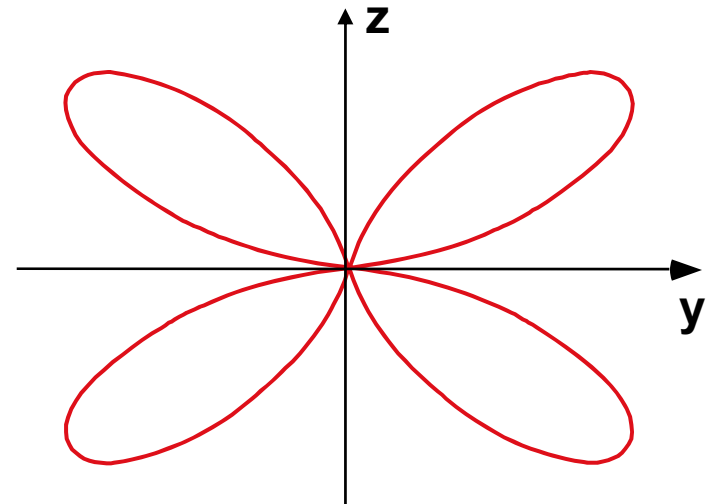
Dipol Antennen mit Länge $2l > \lambda$



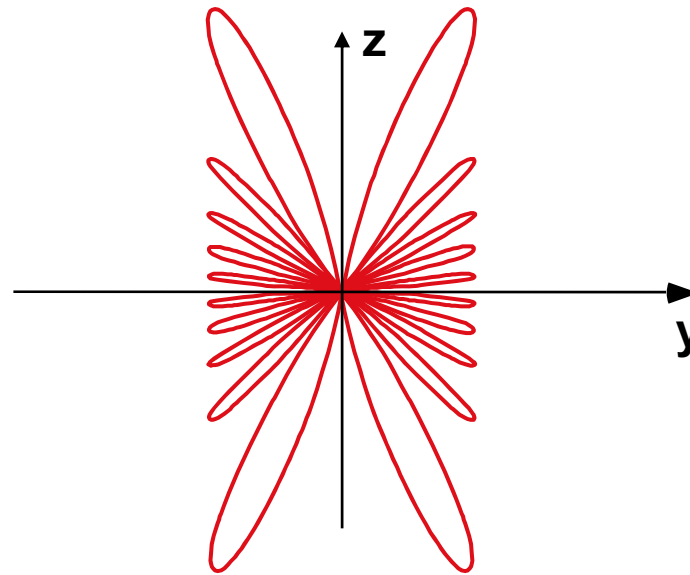
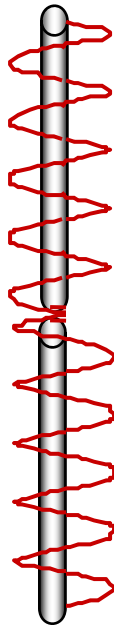
$$2l = 3\lambda / 2$$



$$2l = 2\lambda$$



Dipol Antennen mit Länge $2l \gg \lambda$



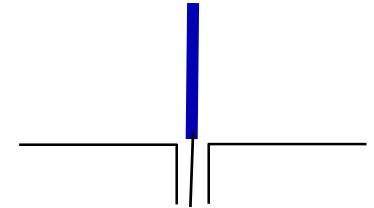
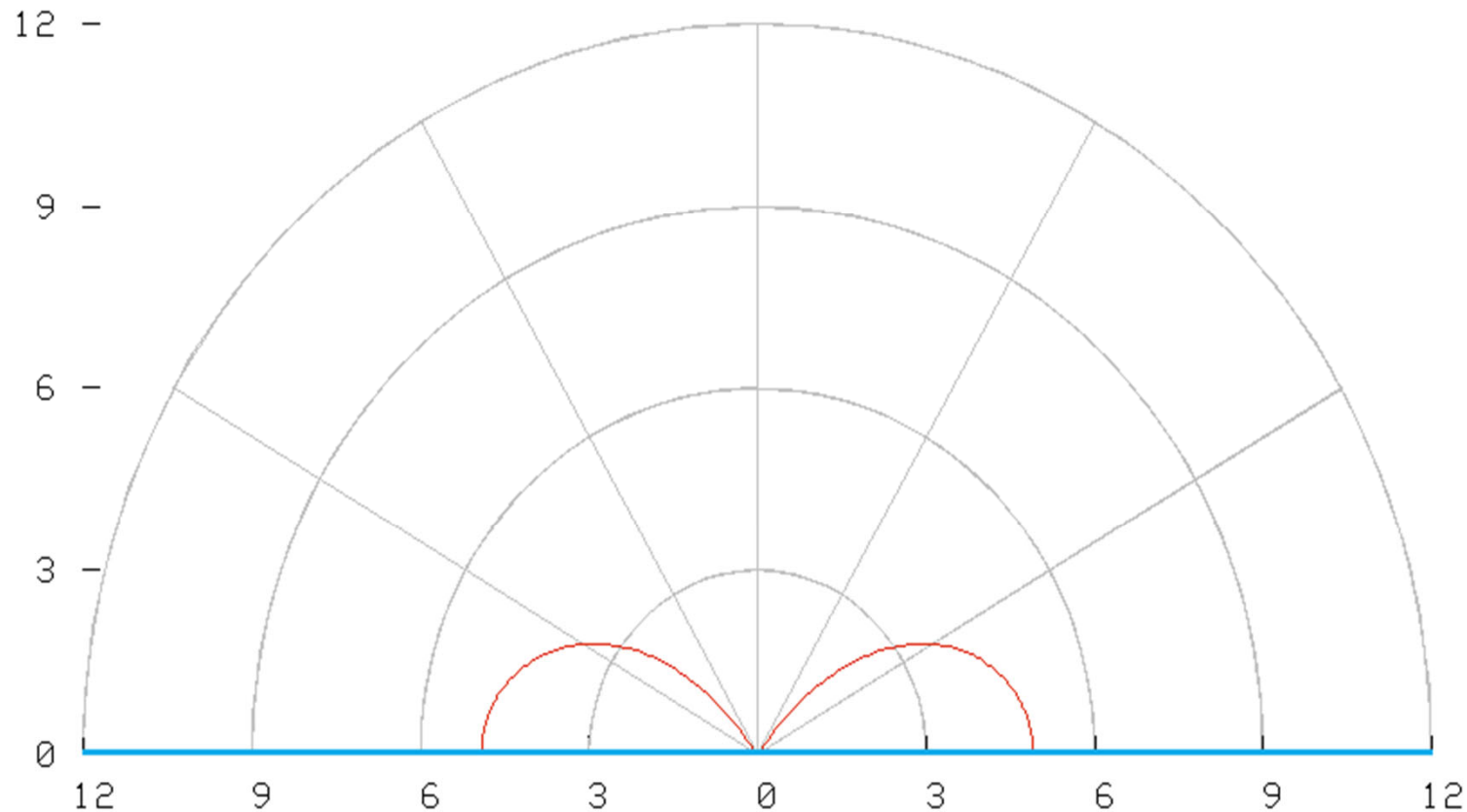
$$2l = 10\lambda$$

Vertikale Fernfeld-Richtcharakteristik eines Monopols

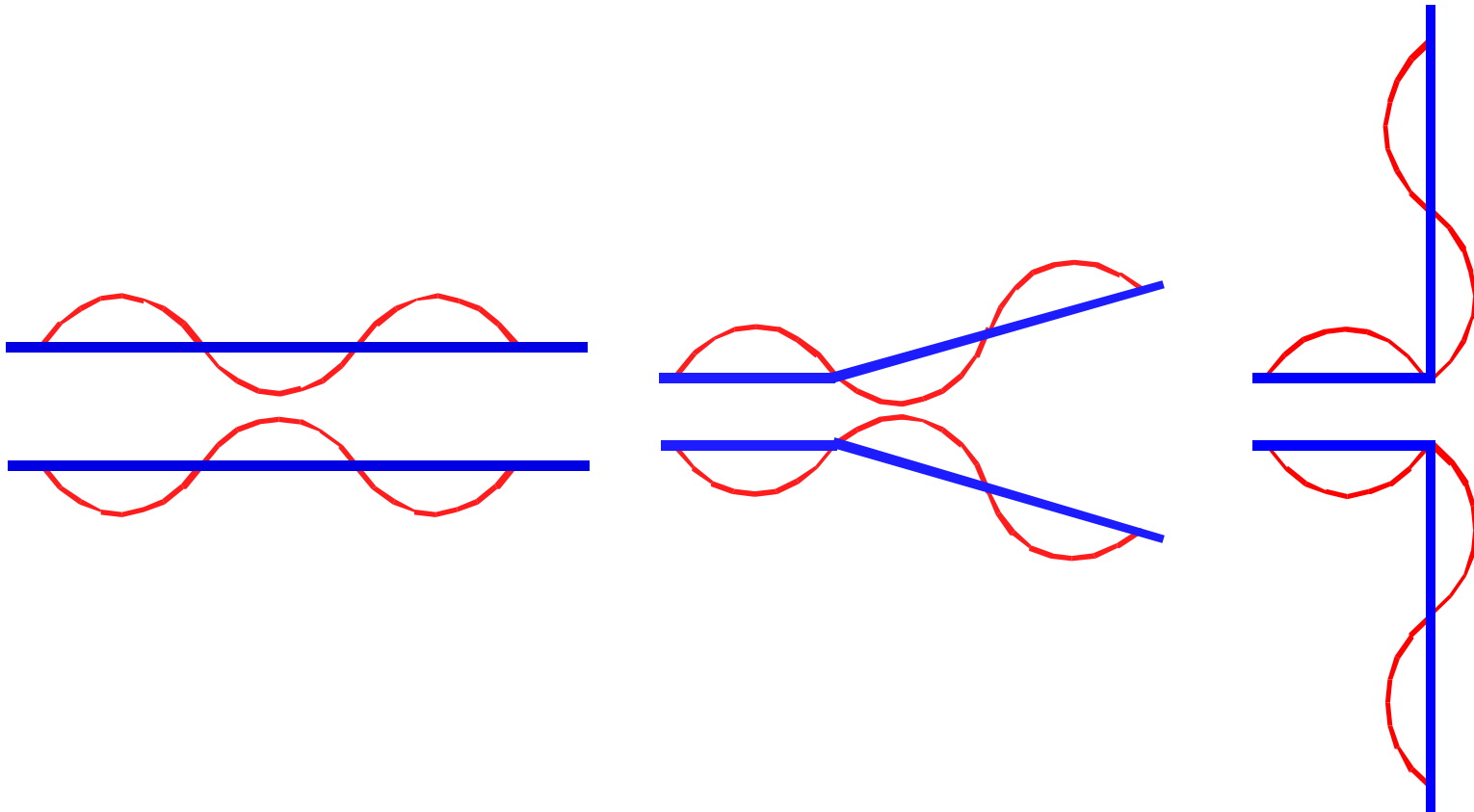
Gewinn in dBi

Länge: $0.1 \lambda < l < 2.5 \lambda$

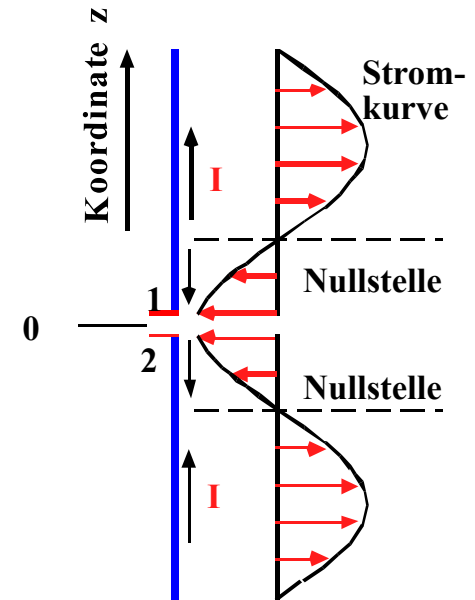
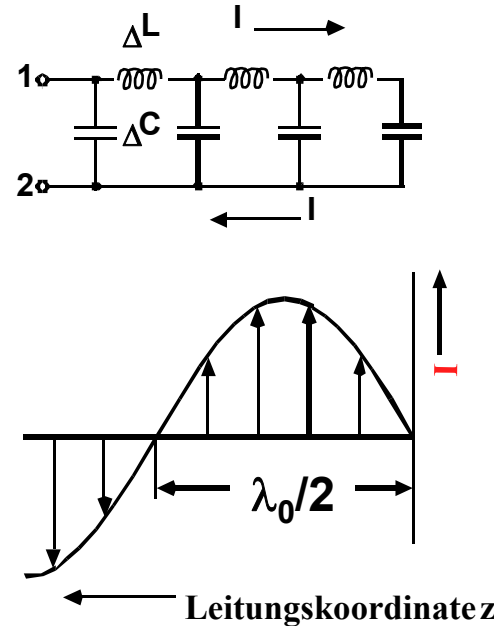
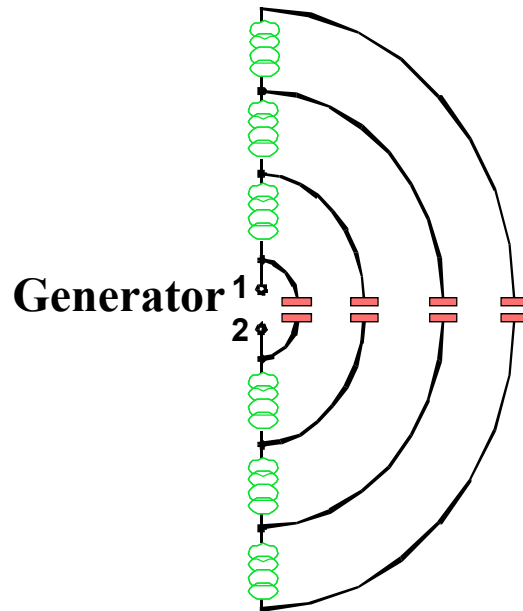
$l = 0.1$ Wellenlängen



Stabantenne als Leitung



Leitungsersatzschaltbild einer Stabantenne



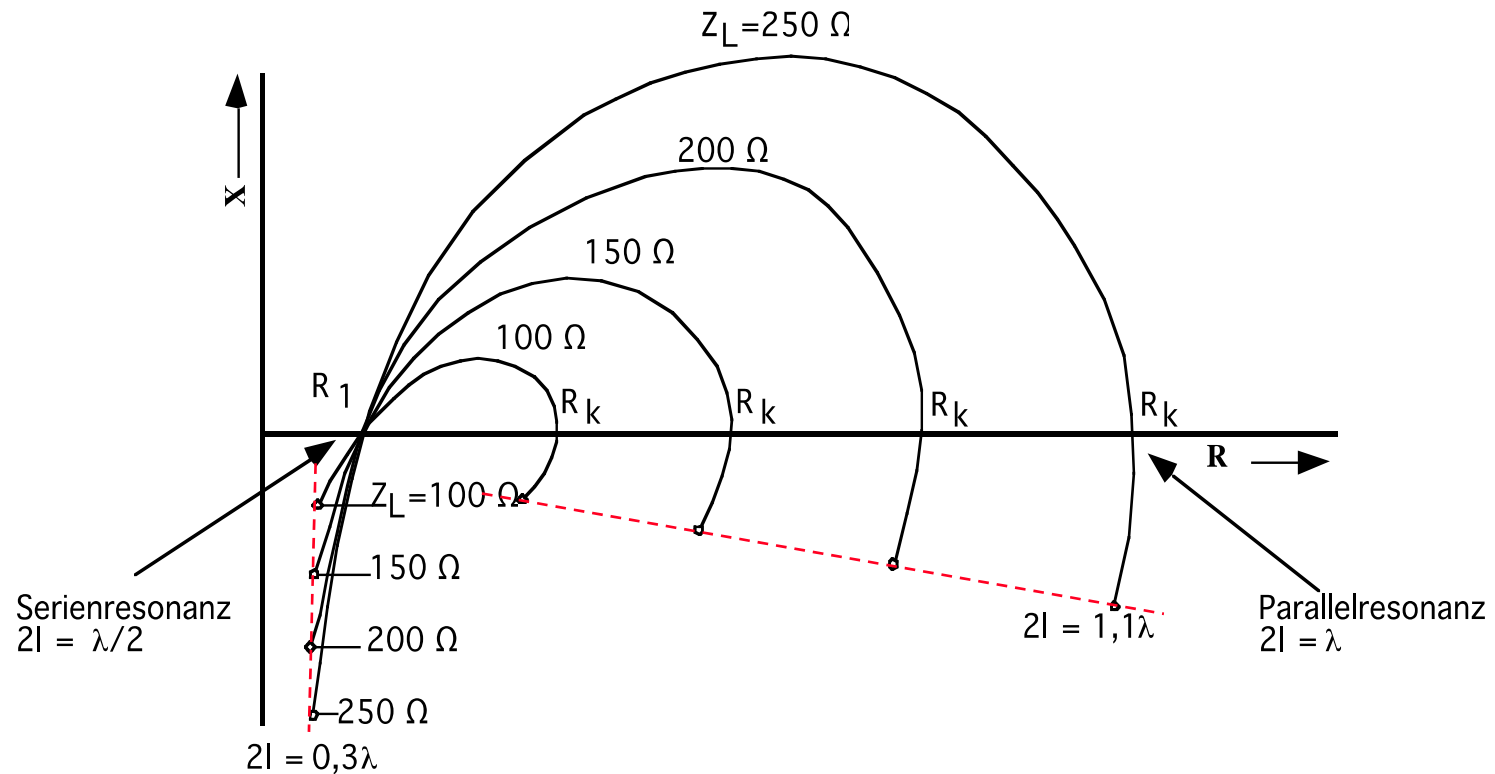
**Näherungsformeln
aus der Literatur:**

$$Z_L = 120\Omega \ln \left[\left(\frac{2l}{a} \right) - 1 \right] \approx 120\Omega \ln \left(1,47 \frac{l}{2a} \right)$$

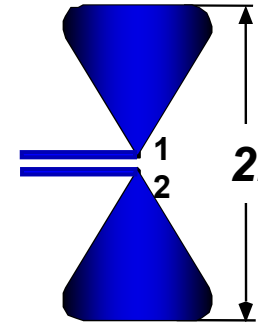
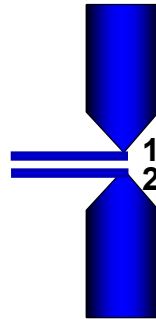
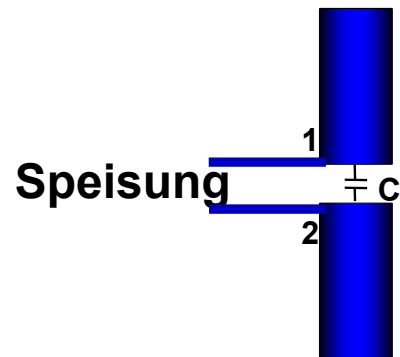
$$Z_L = 60\Omega \ln \left(\frac{l^2}{3a^2} \right) \approx 120\Omega \ln \left(1,15 \frac{l}{2a} \right)$$

Eingangsimpedanz eines Stabstrahlers

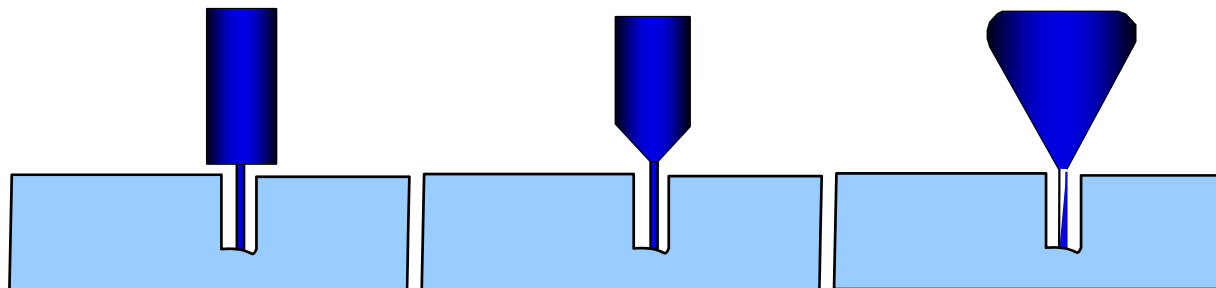
mittlere Wellenwiderstände Z_L



Breitband Monopole und Dipole

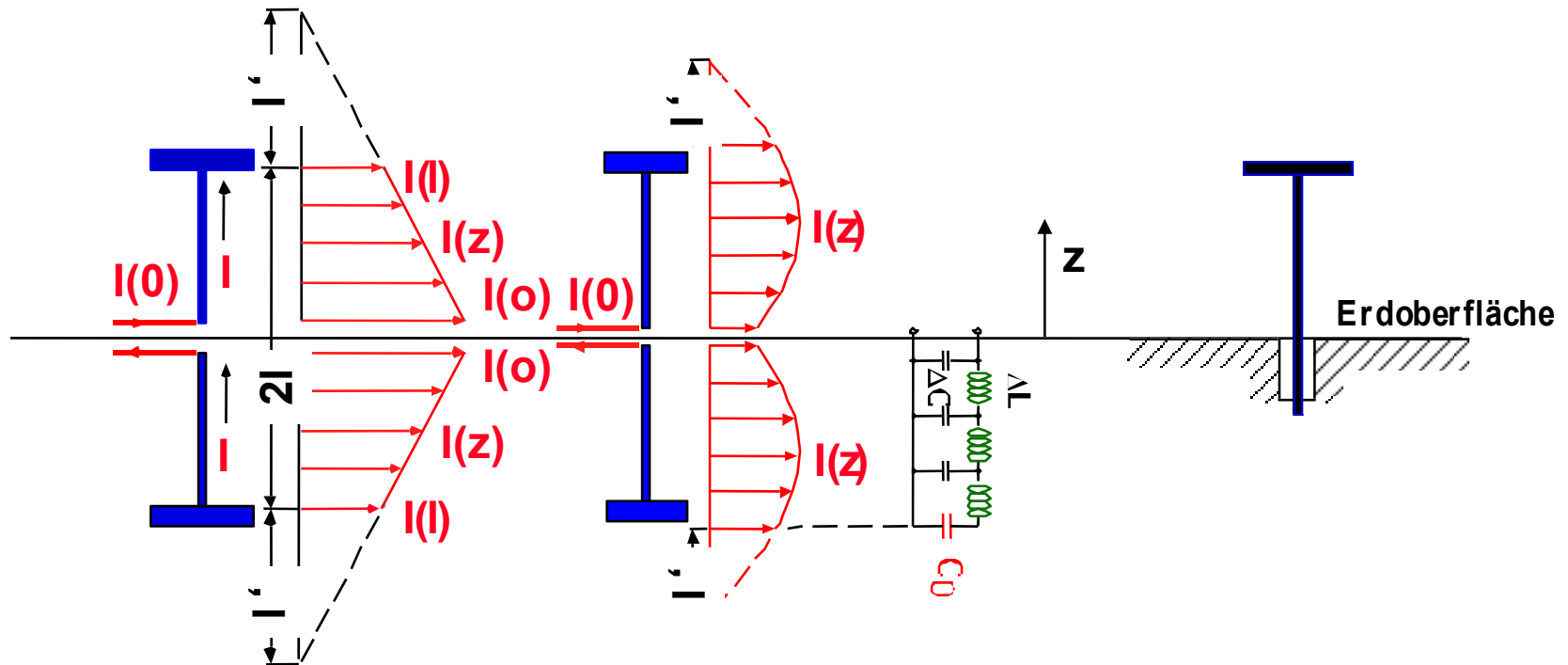


symmetrische
Dipole



Monopole

Kapazitiv belastete Stabstrahler (Mono- und Dipole)



U-Boot Kommunikation Sendeanlage WHV



Höhe: ca. 354 m

Frequenz: ca. 50 kHz

Mastdurchmesser : 2,50 m

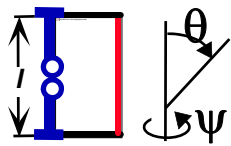
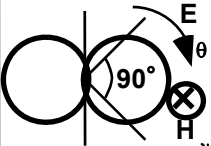
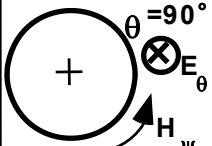
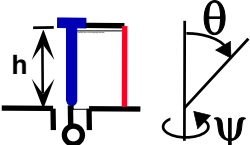
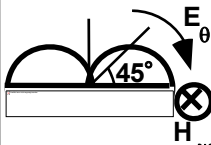
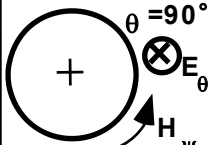
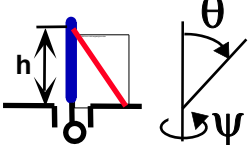
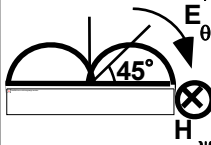
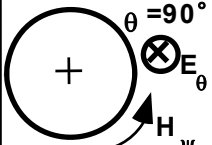
Speisung:

unsymm. 9 m über Grund

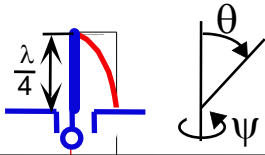
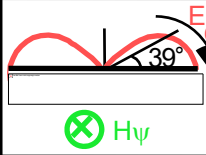
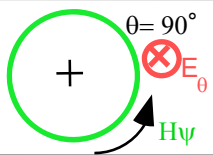
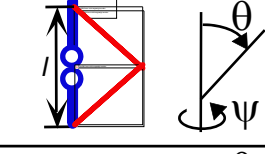
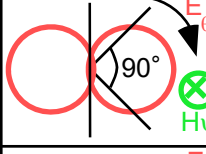
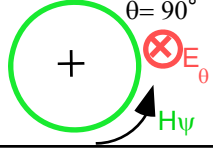
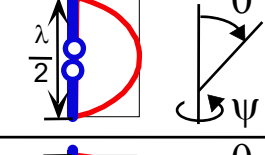
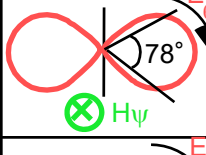
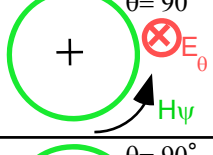
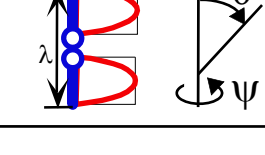
U-Boot Sendeanlage WHV (2 Masten und Zentrale)



Charakteristiken Einfacher Stabantennen I

Antennenart	Darstellung, Belegung	Richtfaktor, Gewinn linear (in dB)	wirksame Antennenfläche	effektive Höhe	Strahlungs-Widerstand	vertikales Richtdiagramm 3dB-Bereich	horizontales Richtdiagramm
Isotrope Antenne	fiktiv	1 ; (0 dB)	$\frac{\lambda^2}{4\pi} = 0,08\lambda^2$	—	—		
Hertzscher Dipol, Dipol mit Endkapazität		1,5 ; (1,8 dB)	$\frac{3\lambda^2}{8\pi} = 0,12\lambda^2$	I	$80 \left(\frac{\pi I}{\lambda}\right)^2 \Omega$		
Kurze Antenne mit Dachkapazität auf leitender Ebene $h \ll \lambda$		3 ; (4,7 dB)	$\frac{3\lambda^2}{16\pi} = 0,06\lambda^2$	h	$160 \left(\frac{\pi h}{\lambda}\right)^2 \Omega$		
kurze Antenne auf leitender Ebene $h \ll \lambda$		3 ; (4,7 dB)	$\frac{3\lambda^2}{16\pi} = 0,06\lambda^2$	$\frac{h}{2}$	$40 \left(\frac{\pi h}{\lambda}\right)^2 \Omega$		

Charakteristiken Einfacher Stabantennen II

Antennenart	Darstellung, Belegung	Richtfaktor, Gewinn Linear (in dB)	Wirksname Antennenfläche	Effektive Höhe	Strahlungs-Widerstand	Vertikales Richt-Diagramm (3dB Bereich)	Horizontales Richt-diagramm
$\lambda/4$ – Antenne auf leitender Ebene		3,28 ; (5,1 dBi)	$0,065\lambda^2$	$\frac{\lambda}{2\pi} = 0,16\lambda$	40 Ω		
Kurzer Dipol $l \ll \lambda$		1,5 ; (1,8 dBi)	$\frac{3\lambda^2}{8\pi} = 0,12\lambda^2$	$\frac{l}{2}$	$20 \left(\frac{\pi l}{\lambda}\right)^2 \Omega$		
$\lambda/2$ - Dipol		1,64 ; (2,1 dBi)	$0,13\lambda^2$	$\frac{\lambda}{\pi} = 0,32\lambda$	73 Ω		
λ - Dipol		2,41 ; (3,8 dBi)	$0,19\lambda^2$	$\gg \lambda$	200 Ω	